

SOLUTIONS & ANSWERS FOR AIEEE-2011 VERSION – P

PART A – CHEMISTRY

1. Ans: 2nd

Sol: RNA contains β-D-ribose while DNA contains β-D-2-deoxyribose.

2. Ans: AlCl₃

Sol: Fajan's rules.
Al³⁺ is the smallest cation and it has high charge.

3. Ans: The stability of hydrides increases from NH₃ to BiH₃ in group 15 of the periodic table.

Sol: Stability of hydrides decreases from NH₃ to BiH₃.

4. Ans: 2, 4, 6-Tribromophenol

Sol: Phenol forms 2, 4, 6-tribromophenol when treated with a mixture of KBr, KBrO₃ and HCl.

5. Ans: 0.086

Sol: Mole fraction of methanol

$$= \frac{\text{moles of methanol}}{\text{total moles}} = \frac{5.2}{5.2 + \frac{1000}{18}}$$

$$= 0.086$$

6. Ans: sp², sp, sp³

Sol: NO₃⁻ – sp², NO₂⁺ – sp and NH₄⁺ – sp³

7. Ans: 804.32 g

Sol: $\Delta T_f = K_f \times \frac{W_2}{M_2} \times \frac{1}{W_1}$

$$6 = 1.86 \times \frac{W_2}{62} \times \frac{1}{4}$$

$$W_2 = 800 \text{ g}$$
 Wt. of glycol required is more than 800 g

8. Ans: p(H₂) = 2 atm and [H⁺] = 1.0 M

Sol: 2H⁺ + 2e⁻ → H₂

$$E_{Cl} = \frac{0.0591}{2} \log \frac{[H^+]^2}{[H_2]}$$

$$[H_2] > [H^+]^2$$

9. Ans: Neutral FeCl₃

Sol: Neutral FeCl₃ solution gives violet colour with phenol.

10. Ans: 2, 2, 2-Trichloroethanol

Sol: 2Cl₃C – CHO + NaOH
 → Cl₃C – CH₂OH + Cl₃C – COONa

11. Ans: Al₂O₃ < MgO < Na₂O < K₂O

Sol: K₂O is more basic than Na₂O. Al₂O₃ is amphoteric.

12. Ans: 743 nm

Sol: $\frac{1}{355} = \frac{1}{680} - \frac{1}{\lambda}$

$$\lambda = 743 \text{ nm}$$

13. Ans: The oxidation state of sulphur is never less than +4 in its compounds

Sol: Sulphur exhibits oxidation state lower than +4 in its compounds.

14. Ans: 38.3 J mol⁻¹ K⁻¹

Sol: $\Delta S = 2.303 nR \log \frac{V_2}{V_1}$

$$= 2.303 \times 2 \times 8.314 \times \log 10$$

$$= 38.3 \text{ J K}^{-1}$$

15. Ans: The complex is an outer orbital complex

Sol: [Cr(NH₃)₆]Cl₃ is not an outer orbital complex.

16. Ans: pentagonal bipyramid

Sol: IF₇ is pentagonal bipyramidal.

17. Ans: 32 times

Sol: 2 times increase for 10°C
 2⁵ = 32 times increase for 50°C

18. Ans: CH₃CH₂CH(Cl)CO₂H

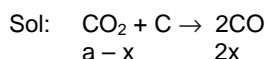
Sol: Presence of Cl having –I effect on the α-carbon makes 2-chlorobutanoic acid the strongest acid among the given compounds.

19. Ans: 2-Pentanone

Sol:
$$\text{CH}_3\text{---}\overset{\text{O}}{\parallel}\text{C}\text{---}\text{CH}_2\text{---}\text{CH}_2\text{---}\text{CH}_3 \rightleftharpoons$$

$$\text{CH}_3\text{---}\overset{\text{OH}}{\mid}\text{C}=\text{CH}\text{---}\text{CH}_2\text{---}\text{CH}_3$$
 ketoform
 enol form

20. Ans: 1.8 atm



$$\begin{aligned} a &= 0.5 \text{ atm} \\ a + x &= 0.8 \text{ atm} \\ x &= 0.3 \text{ atm} \end{aligned}$$

$$K_p = \frac{P_{\text{CO}}^2}{P_{\text{CO}_2}} = \frac{(0.6)^2}{0.2} = 1.8 \text{ atm}$$

21. Ans: Availability of 4f electrons results in the formation of compounds in +4 state for all the members of the series

Sol: All the lanthanoids does not exhibit +4 oxidation state.

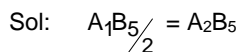
22. Ans: a for $\text{Cl}_2 >$ a for C_2H_6 but b for $\text{Cl}_2 <$ b for C_2H_6

Sol: 'a' is a measure of attraction between the molecules and 'b' the size of the molecules.

23. Ans: 2.82 BM

Sol: There are two unpaired electrons in $[\text{NiCl}_4]^{2-}$ hence the paramagnetic moment is 2.82 BM.

24. Ans: A_2B_5



25. Ans: $4f^7 5d^1 6s^2$

Sol: The outer electronic configuration of ${}_{64}\text{Gd}$ is $4f^7 5d^1 6s^2$

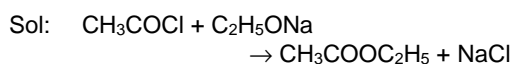
26. Ans: BF_6^{3-}

Sol: Boron cannot form BF_6^{3-} since boron has no available d-orbitals.

27. Ans: a vinyl group

Sol: Formation of HCHO in ozonolysis shows the presence of $\text{CH}_2 = \text{CH} -$ group.

28. Ans: Ethyl ethanoate



29. Ans: $\alpha = \frac{i-1}{(x+y-1)}$

Sol: $i = 1 - \alpha + n\alpha$; $n = x + y$
$$\alpha = \frac{i-1}{x+y-1}$$

30. Ans: Acetaldehyde

Sol: Acetaldehyde reduces tollens's reagent to metallic silver on warming.

PART - B - PHYSICS

31. Ans: 8.4 kJ

Sol: $\Delta U = mC\Delta T$
 $= 4184 \times 20 \times 0.1$
 $= 8.4 \text{ kJ}$

32. Ans: 20 min

Sol: $N = \frac{N_0}{2^{t/T_{1/2}}}$
 $\frac{N_0}{3} = \frac{N_0}{2^{t_2/20}} \Rightarrow t_2 = 20 \frac{\log 3}{\log 2}$
 $N_0 \frac{2}{3} = \frac{N_0}{2^{t_1/20}} \Rightarrow t_1 = \frac{20(\log 3 - \log 2)}{\log 2}$
 $t_2 - t_1 = \frac{20}{\log 2} (\log 3 - \log 3 + \log 2)$
 $= 20 \text{ min}$

33. Ans: $\left(\frac{M+m}{M}\right)^{1/2}$

Sol: $Mv_1 = (M+m)v_2$
 $\frac{v_1}{v_2} = \frac{M+m}{M}$
 $\frac{1}{2}(M+m)v_2^2 = \frac{1}{2}KA_2^2$
 $\frac{1}{2}Mv_1^2 = \frac{1}{2}KA_1^2$
 $\frac{1}{2}Mv_1^2 = \frac{1}{2}KA_1^2$
 $\Rightarrow \frac{A_1^2}{A_2^2} = \frac{M}{M+m} \left(\frac{M+m}{M}\right)^2$
 $= \frac{M+m}{M}$
 $\therefore \frac{A_1}{A_2} = \left(\frac{M+m}{M}\right)^{1/2}$

34. Ans: 108.8 eV

Sol: $\frac{13.6 Z^2}{n^2} = 13.6 \times 9 \left[1 - \frac{1}{9}\right]$
 $= 13.6 \times 9 \times \frac{8}{9}$
 $= 108.8 \text{ eV}$

35. Ans: Wave moving in -x direction with speed $\sqrt{\frac{b}{a}}$

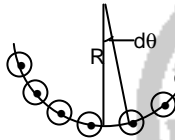
Sol: $y(x, t) = e^{-(\sqrt{a}x + \sqrt{b}t)^2}$
 This is of the form $y(x, t) = f(x + vt)$, where
 $v = \frac{\sqrt{b}}{\sqrt{a}}$ travels in negative x direction.

36. Ans: $2.7 \times 10^6 \Omega$

Sol: $V = V_0(1 - e^{-t/RC})$
 $120 = 200(1 - e^{-t/RC})$
 $e^{-t/RC} = \frac{2}{5}$
 $e^{t/RC} = 2.5$
 $\frac{t}{RC} = 0.4 \times 2.5 \times 2.303$
 $\Rightarrow R = 2.7 \times 10^6 \Omega$

37. Ans: $\frac{\mu_0 I}{\pi^2 R}$

Sol: $B = \frac{I}{\pi R} R d\theta \frac{\mu_0}{2\pi R} \sin \theta$



$= \frac{\mu_0 I}{2\pi^2 R} \int_0^{\pi/2} \sin \theta d\theta$
 $= \frac{\mu_0 I}{\pi^2 R}$

38. Ans: 372 K and 310 K

Sol: $1 - \frac{T_2}{T_1} = \frac{1}{6}$
 $1 - \frac{T_2 - 62}{T_1} = \frac{1}{3}$
 $\frac{T_2}{T_1} = \frac{5}{6}$
 $\frac{T_2 - 62}{T_1} = \frac{2}{3}$
 $\frac{T_2}{T_2 - 62} = \frac{5}{4}$
 $4T_2 = 5T_2 - 310$
 $T_2 = 310 \text{ K}$
 $\Rightarrow T_1 = 372 \text{ K}$

39. Ans: 2 s

Sol: $\frac{dv}{dt} = -2.5\sqrt{v}$

$\frac{dv}{\sqrt{v}} = -2.5 dt$
 $\Rightarrow -2.5t = \left[2\sqrt{v} \right]_{6.25}^0$
 $t = \frac{2\sqrt{6.25}}{2.5}$
 $= \frac{2 \times 2.5}{2.5} = 2$

40. Ans: $-6 \epsilon_0 a$

Sol: $V = ar^2 + b$
 $E = -\frac{dV}{dr} = -2ar$
 $4\pi r^2 \cdot E = \frac{Q}{\epsilon_0}$
 $Q = -4\pi r^2 \cdot 2ar \cdot \epsilon_0$
 $\rho = \frac{-8\pi ar^3 \epsilon_0}{\frac{4}{3}\pi r^3}$
 $= -6 \epsilon_0 a$

41. Ans: $\frac{1}{15} \text{ m s}^{-1}$

Sol: $\frac{1}{v} + \frac{1}{-2.8} = \frac{1}{0.2}$
 $\Rightarrow \frac{1}{v} = \frac{15}{2.8}$
 $v = \frac{2.8}{15}$
 $\frac{v}{u} = \frac{1}{15}$
 $\frac{v^2}{u^2} = \frac{1}{15^2}$
 $\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$
 $\Rightarrow \frac{dv}{dt} = -\frac{v^2}{u^2}$
 $\left| \frac{dv}{dt} \right| = \frac{v^2}{u^2} \cdot \frac{du}{dt}$
 $= \frac{1}{15^2} \times 15 = \frac{1}{15} \text{ m s}^{-1}$

42. Ans: Increases by 0.2%

Sol: $R \propto \lambda^2$
 $R' \propto \lambda'^2$
 $\propto (1.001)^2 \lambda^2$
 $\frac{\Delta R}{R} = 0.002$
 $\therefore 0.002 \times 100$
 $= 0.2\%$

43. Ans: $\frac{n_1 T_1 + n_2 T_2 + n_3 T_3}{n_1 + n_2 + n_3}$

Sol: $P_1 V = n_1 K T_1$
 $P_2 V = n_2 K T_2$
 $P_3 V = n_3 K T_3$
 $\frac{1}{2} m v^2 = \frac{3}{2} K T_1 n_1 + \frac{3}{2} K T_2 n_2 + \frac{3}{2} K T_3 n_3$
 $= \frac{3}{2} K (n_1 + n_2 + n_3) T$
 $T = \frac{n_1 T_1 + n_2 T_2 + n_3 T_3}{n_1 + n_2 + n_3}$

44. Ans: $v \propto x$

Sol: $T \cos \theta = mg$
 $T \sin \theta = F$
 $\tan \theta = \frac{F}{mg}$
 $\frac{x}{2\lambda} = \frac{F}{mg}$
 $F \propto x$
 $\int v dv \propto \int x dx$
 $v^2 \propto x^2$
 $v \propto x$

45. Ans: $0.4\pi \text{ mJ}$

Sol: $E = T \cdot 8\pi (r_2^2 - r_1^2)$
 $= 8\pi T \left(\frac{25}{10^4} - \frac{9}{10^4} \right)$
 $= 8 \times 16 \times \pi \times 0.03 \times 10^{-4}$
 $= 0.4\pi \text{ mJ}$

46. Ans: $\frac{\pi}{4} \sqrt{LC}$

Sol: $q' = q_0 \cos \omega t$
 $E = \frac{q_0^2}{2C}$
 $\frac{E}{2} = \frac{1}{2} \frac{q_0^2}{2C}$
i.e. $q' = \frac{q_0}{\sqrt{2}}$
 $\frac{q_0}{\sqrt{2}} = q_0 \cos \omega t$
 $\Rightarrow \omega t = \frac{\pi}{4}$
 $t = \frac{\pi}{4} \sqrt{LC}$

47. Ans: $\frac{-9Gm}{r}$

Sol: $\frac{Gm}{x^2} = \frac{G4m}{(r-x)^2}$

$$\frac{(r-x)^2}{x^2} = 4$$

$$r-x = 2x$$

$$x = \frac{r}{3}$$

$$V = \frac{-Gm}{r} - \frac{G4m}{2r}$$

$$= -\frac{Gm}{r} (3+6)$$

$$= \frac{-9Gm}{r}$$

48. Ans: First increases and then decreases.

Sol: Angular momentum is conserved.
I decreases ω increases then I increases ω decreases.

49. Ans: 45°

Sol: $\mu_1 [\hat{N} \times K_1] = \mu_2 [\hat{N} \times K_2]$. But plane of separation need to be XY.

50. Ans: $\frac{\pi}{2}$

Sol: Particle 1 is at equilibrium position ($\phi = 0$).
Particle 2 is at maximum position. ($\phi = \frac{\pi}{2}$)

51. Ans: Statement-1 is true, Statement-2 is true and Statement -2 is not the correct explanation of statement - 1

Sol: Statement-1 is true, Statement-2 is true and Statement -2 is not the correct explanation of statement - 1

52. Ans: $\frac{1}{2} \frac{Mv^2(\gamma-1)}{R}$

Sol: Volume is constant

$$C_v = \frac{R}{(\gamma-1)}$$

$$KE = \frac{1}{2} Mv^2$$

$$\Delta Q = nC_v \Delta \theta = 1 \times C_v \Delta \theta$$

$$\therefore \Delta \theta = \frac{KE}{C_v} = \frac{1}{2} \frac{Mv^2(\gamma-1)}{R}$$

53. Ans: 0.052 cm

Sol: $LC = \frac{1}{100} = 0.01 \text{ mm}$
 Reading = PSR \times pitch + CSR \times LC
 $= 0 + 52 \times 0.01$
 $= 0.52 \text{ mm}$
 $= 0.052 \text{ cm}$

54. Ans: 0.15 mV

Sol: $\varepsilon = B\lambda v$
 $= 5 \times 10^{-5} \times 2 \times 1.50$
 $= 0.15 \text{ mV}$

55. Ans: Statement 1 is true. Statement 2 is true. and statement 2 is the correct explanation for statement – 1.

Sol: Statement 1 is true. Statement 2 is true. and statement 2 is the correct explanation for statement – 1.

56. Ans: $\frac{2}{3} g$

Sol: $mg - T = ma$
 $TR = \frac{mR^2}{2} \cdot \frac{a}{R}$
 $\Rightarrow mg = \frac{3}{2} ma$
 $\Rightarrow a = \frac{2}{3} g$

57. Ans: $\frac{\pi v^4}{g^2}$

Sol: $R_{\max} = \frac{v^2}{g}$
 Area = $\pi(R_{\max})^2$
 $= \frac{\pi v^4}{g^2}$

58. Ans: Statement – 1 is false, Statement-2 is true.

Sol: If $v \Rightarrow 2v$,
 $V_0' > 2V_0$, well known result
 \Rightarrow Statement 1 is wrong.
 Statement 2 is true.

59. Ans: more than 3 but less than 6.

Sol: $\tau = Fr = 40t - 10t^2$
 $\alpha = \frac{\tau}{I} = 4t - t^2$

$$\frac{d\omega}{dt} = 4t - t^2 \Rightarrow \omega = 2t^2 - \frac{t^3}{3}$$

(Θ At $t = 0$, $\omega = 0$)

At $t = 6 \text{ s}$, ω again become zero

$$\omega = \frac{d\theta}{dt} = 2t^2 - \frac{t^3}{3} \Rightarrow \theta = \frac{2t^3}{3} - \frac{t^4}{12}$$

$\therefore \theta$ in 6 s = $(144 - 108) = 36 \text{ rad}$

$$\Rightarrow N = \frac{\theta}{2\pi} = \frac{36}{2\pi} = 5.72 \text{ rotation.}$$

60. Ans: $3.6 \times 10^{-3} \text{ m}$

Sol: $P_0 + \frac{1}{2} \rho v_1^2 + \rho gh$
 $= P_0 + \frac{1}{2} \rho v_2^2$
 $\Rightarrow 2gh = (v_2^2 - v_1^2)$
 $\Rightarrow 2gh + v_1^2 = v_2^2$;
 $v_1 = 0.4 \text{ m s}^{-1}$, $h_2 = 0.2 \text{ m}$
 $\Rightarrow v_2 = 2.0396 \text{ m s}^{-1}$
 $A_1 v_1 = A_2 v_2 \Rightarrow d_2^2 = \frac{d_1^2 v_1}{v_2}$

$$\Rightarrow d_2 = d_1 \sqrt{\frac{v_1}{v_2}}$$

$$= 8 \times 10^{-3} \times \sqrt{\frac{0.4}{2.0396}}$$

$$\approx 3.6 \times 10^{-3} \text{ m}$$

Part – C – Mathematics

61. Ans: $\beta \in (1, \infty)$

Sol: If $1 + ai$ is root (a , real)
 Then $(1 + ia)^2 + \alpha(1 + ia) + \beta = 0$
 $2a + \alpha = 0 \Rightarrow \alpha = -2a \neq 0$
 $1 - a^2 + \alpha + \beta = 0$
 $1 - a^2 + \beta = 0$
 $\beta = a^2 + 1 > 1 \therefore \beta \in (1, \infty)$

62. Ans: $\pi \log 2$

Sol: $I = 8 \int_0^1 \frac{\log(1+x)}{1+x^2}$
 $= 8 \int_0^{\pi/4} \text{Log}(1 + \tan \theta) d\theta$
 $= \pi \log 2$

63. Ans: $-\left(\frac{d^2y}{dx^2}\right)\left(\frac{dy}{dx}\right)^{-3}$

Sol: $\frac{d^2x}{dy^2} = \frac{d}{dy} \left(\frac{dx}{dy}\right)$

$$\begin{aligned}
 &= \frac{d}{dy} \left[\frac{1}{\frac{dy}{dx}} \right] \\
 &= \frac{-1}{\left(\frac{dy}{dx}\right)^2} \cdot \frac{d}{dy} \left(\frac{dy}{dx} \right) \\
 &= \frac{-1}{\left(\frac{dy}{dx}\right)^2} \frac{d^2y}{dx^2} \left(\frac{dx}{dy} \right) \\
 &= - \left(\frac{d^2y}{dx^2} \right) \left(\frac{dy}{dx} \right)^{-3}
 \end{aligned}$$

64. Ans: $I - \frac{kT^2}{2}$

Sol: $\frac{dv(t)}{dt} = -k(T-t)$
 $V(t) = \int -k(T-t) dt$
 $\frac{k(T-t)^2}{2} + C$
 $t = 0, V(t) = I$
 $\Rightarrow I = \frac{kT^2}{2} + C$
 $C = I - \frac{kT^2}{2}$
 Therefore,
 $V(t) = \frac{k(T-t)^2}{2} + I - \frac{kT^2}{2}$
 $\Rightarrow V(T) = 0 + I - \frac{kT^2}{2}$
 $= I - \frac{kT^2}{2}$

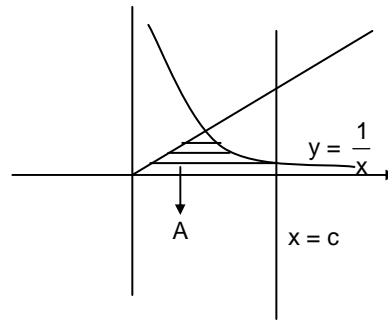
65. Ans: -144

Sol: $(1 - x - x^2 + x^3)^6 = (1-x)^6 (1-x^2)^6$
 $= (1 - 6x + \dots - 20x^3 \dots - 6x^5) x$
 $(1 - 6x^2 + 75x^4 - 20x^6 \dots)$
 $= 120 - 300 + 36$
 $= 156 - 300 = -144$

66. Ans: local maximum at π and local minimum at 2π

Sol: $f'(x) = \sqrt{x} \sin x$
 $f''(x) = \frac{2x \cos x + \sin x}{2\sqrt{x}}$
 $f'(x) = 0 \Rightarrow x = n\pi, n \in \mathbb{Z}$
 ie., $x = \pi, 2\pi$ in $(0, \frac{5\pi}{2})$
 $f''(\pi) < 0$ and $f''(2\pi) > 0$
 $\therefore f(x)$ has maximum at $x = \pi$
 And minimum at $x = 2\pi$

67. Ans: $\frac{3}{2}$ square units



Sol: $y = x$
 $y = \frac{1}{x} \Rightarrow x^2 = 1$
 $\Rightarrow x = 1 (x > 0)$
 $y = \frac{1}{x}, x = e \Rightarrow x = e$

\therefore area $A = \int_1^e \left(x - \frac{1}{x}\right) dx$
 $= \frac{e^2 - 1}{2} - \log e$
 $= \frac{e^2 - 3}{2}$

Required area = $\frac{1}{2} \cdot e^2 - \frac{e^2 - 3}{2} = \frac{3}{2}$

68. Ans: Statement-1 is true, Statement-2 is false.

Sol: P is (-2, -2) and Q (-1, 2) since R bisect $\angle POQ$, $PR \perp RQ = OP : OQ$
 $= \sqrt{4+4} : \sqrt{1+4} = \sqrt{8} : \sqrt{5}$
 \therefore Statement 1 is true
 But statement 2 is false.

69. Ans: $p = -\frac{3}{2}, q = \frac{1}{2}$

Sol: $f(x) = \frac{\sin(p+1)x + \sin x}{x}, x < 0$
 $= q, x = 0$
 $\frac{\sqrt{x+x^2} - \sqrt{x}}{x^{3/2}}, x > 0$

is continuous.

$\Rightarrow p + 1 + 1 = q = \lim_{x \rightarrow 0} \frac{x}{x^{3/2}(\sqrt{x+x^2} + \sqrt{x})}$
 $= \frac{1}{2}$

$\therefore p = -\frac{3}{2}, q = \frac{1}{2}$

70. Ans: $\frac{2}{3}$

Sol: The angle is $\sin^{-1} \frac{3}{\sqrt{14}}$
 $\therefore \frac{1+4+3\lambda}{\sqrt{(1+4+\lambda^2)(1+4+9)}} = \frac{3}{\sqrt{14}}$
 $14(3\lambda+5)^2 = 9 \times 14(5+\lambda^2)$
 $9\lambda^2 + 30\lambda + 25 = 9\lambda^2 + 45$
 $\Rightarrow 30\lambda = 20 \Rightarrow \lambda = \frac{2}{3}$

71. Ans: $(-\infty, 0)$

Sol: $|x| - x > 0$
 $\Rightarrow |x| > x$
 $\Rightarrow x \in (-\infty, 0)$

72. Ans: $\frac{3\sqrt{2}}{8}$

Sol: Slope of the line perpendicular to $y - x = 1$ is (-1)
Hence $t = 1$
Point on the parabola corresponding to $t = 1$ is
 $\Rightarrow \left(\frac{1}{4}, \frac{1}{2}\right)$

\therefore shortest distance = $\frac{\frac{1}{4} - \frac{1}{2} + 1}{\sqrt{2}} = \frac{3\sqrt{2}}{8}$

73. Ans: 21 months

Sol: Total savings = 11040
Savings in the first 2 months = 400
Hence, savings in the next n months = 10640

We have

$$\frac{n}{2}[400 + (n-1)40] = 10640$$

$$[200 + (n-1)20]n = 10640$$

$$200n + 20n^2 - 20n = 10640$$

$$20n^2 + 180n - 10640 = 0$$

$$n^2 + 9n - 532 = 0$$

$$n = \frac{9 \pm \sqrt{81 + 2128}}{2}$$

$$= \frac{-9 \pm \sqrt{2209}}{2} = \frac{-9 \pm 47}{2}$$

$$= 19$$

Therefore, answer is 21 months

74. Ans: $\sim (Q \leftrightarrow (P \wedge \sim R))$

Sol: The given statement is
 $(P \wedge \sim R) \leftrightarrow Q \equiv Q \leftrightarrow (P \wedge \sim R)$
 \therefore The required negative is
 $\sim [Q \leftrightarrow (P \wedge \sim R)]$

75. Ans: $(1, 1)$

Sol: $(1 + \omega)^7 = A + B\omega$
 $(-\omega^2)^7 = A + B\omega$
 $-\omega^{14} = A + B\omega$
 $-\omega^2 = A + B\omega$
 $1 + \omega = A + B\omega$
 $\therefore A = 1 \quad B = 1$
 $\therefore (1, 1)$

76. Ans: -5

Sol: $|a| = |b| = 1 \quad a, b = 0$
 $(2a - b) \cdot ((a \times b) \times (a + 2b))$
 $= (2a - b) \times$
 $[(a \cdot a) b - (a \cdot b) a + (2b \cdot a) b - (2b \cdot b)]$
 $(2a - b) \cdot (b - 2a) = -5$

77. Ans: 7

Sol: $\frac{dy}{dx} = y + 3$
 $\frac{dy}{y+3} = dx$
 $\log(y+3) = x + c$
 $\therefore y + 3 = c e^x$
 $x = 0 \quad y = 2 \Rightarrow c = 5$
 $\therefore y = 5 e^x - 3$
 $\therefore y(\log 2) = 5 e^{\log 2} - 3$
 $= 5 \times 2 - 3 = 7$

78. Ans: $3x^2 + 5y^2 - 32 = 0$

Sol: $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$
 $\frac{9}{a^2} + \frac{1}{b^2} = 1$
 $\frac{1}{b^2} = 1 - \frac{9}{a^2}$
 $\frac{1}{a^2(1 - \frac{9}{a^2})} = \frac{a^2 - 9}{a^2}$
 $a^2 - 9 = \frac{3}{5}$
 $a^2 = 9 + \frac{3}{5} = \frac{32}{5}$
 $b^2 = a^2 \times \frac{3}{5} = \frac{32}{5} \times \frac{3}{5} = \frac{32}{5}$
Equation of the ellipse is
 $\frac{x^2}{\frac{32}{5}} + \frac{y^2}{\frac{32}{5}} = 1$
 $\frac{3x^2}{32} + \frac{5y^2}{32} = 1$
 $3x^2 + 5y^2 - 32 = 0$

79. Ans: 4

Sol: Median = $\frac{25a + 26b}{2}$
 $= \frac{51a}{2}$

Numerical value of the sum of the derivation

$$= \left| 2a \left\{ \frac{1}{2} + \frac{3}{2} + \frac{5}{2} + \dots + \frac{49}{2} \right\} \right|$$

$$= \left| \frac{2a \times 25^2}{2} \right| = |25^2 a|$$

$$\text{Mean derivation about median} = \left| \frac{25^2 a}{50} \right|$$

$$\left| \frac{25^2 a}{50} \right| = 50$$

$$|a| = \frac{50 \times 50}{25 \times 25} = 4$$

80. Ans: Does not exist

Sol: $\lim_{x \rightarrow 2} \sqrt{2} \left| \frac{\sin(x-2)}{(x-2)} \right|$
Limit does not exist

81. Ans: Statement-1 is true, Statement-2 is true;
Statement -2 is a correct explanation for Statement-1.

Sol: $x_1 + x_2 + x_3 + x_4 = 6$
 $x_i \geq 0$
no. of ways = 9C_3
 S_2 is true
 S_1 is true
 S_1 follows from S_2

82. Ans: Statement-1 is true, Statement-2 is true;
Statement -2 is **not** a correct explanation for Statement-1.

Sol: $A = (x, y) \quad y - x \in Z$
 $B = (x, y) \quad x = \alpha y$ for rational α
 $A : x - x = 0 \in Z \Rightarrow (x, x) \in A$ reflexive
 $y - x \in Z \Rightarrow x - y \in Z$
 $\Rightarrow (y, x) \in A$ symmetric
 $y - x \in Z$ and $z - y \in Z \Rightarrow z - x \in Z$
 $\therefore (x, z) \in A$ transitive
A is equivalence relation
Statement - 1 is true
B: $x = 1, x \Rightarrow (x, x) \in B$ reflexive
 $x = \alpha y \Rightarrow y = \frac{1}{\alpha} x \quad \therefore (y, x) \in B$
symmetric
 $x = \alpha y$ and $y = \alpha z \Rightarrow x = \alpha^2 z$
 $\therefore (x, z) \in B$ transitive
B is equivalence relation
Statement - 2 is true but I does not follow from 2.

83. Ans: $\left[0, \frac{1}{2} \right]$

Sol: $1 - P^5 \geq \frac{31}{32}$
 $P^5 \leq 1 - \frac{31}{32}$

$$\leq \frac{1}{32}$$

$$P \leq \frac{1}{2} = \left[0, \frac{1}{2} \right]$$

Choice (3)

84. Ans: $|a| = c$

Sol: Two circle should touch each other
Centres are $\left(\frac{a}{2}, 0 \right)$ and $(0, 0)$
 \therefore also second circle passes through $(0, 0)$
 $\therefore c = a \Rightarrow |a| = c$

85. Ans: Statement-1 is true, Statement-2 is true;
Statement -2 is **not** a correct explanation for Statement-1.

Sol: if $AB = BA$
 $(AB)^T = A^T B^T$
 $\Rightarrow AB$ is symmetric
Statement-2 is true
 $(ABA)^T = A^T B^T A^T$
Take $A = I$ and $B =$ some non - symmetric
 $\therefore ABA$ always
 $\therefore A(BA)$ and $(AB)A$ are symmetric
Statement-1 is true nut does not depend on Statement-2

86. Ans: $P(C|D) \geq P(C)$

Sol: $P(C|D) = \frac{P(CD)}{P(D)}$
 $= \frac{P(C)}{P(D)}$
 $\geq P(C)$

87. Ans: $\bar{c} - \frac{\bar{a} \cdot \bar{c}}{\bar{a} \cdot \bar{b}} \bar{b}$

Sol: $\bar{b} \times \bar{c} = \bar{b} \times \bar{d}$
 $\bar{a} \cdot \bar{d} = 0$
 $\bar{b} \times (\bar{c} - \bar{d}) = 0$
 \bar{b} and $(\bar{c} - \bar{d})$ are collinear
 $\bar{b} = k(\bar{c} - \bar{d})$
 $\bar{a} \cdot \bar{b} = k(\bar{a} \cdot \bar{c} - \bar{a} \cdot \bar{d})$
 $k \left[\bar{c} - \bar{c} \right]$
 $k = \frac{\bar{a} \cdot \bar{b}}{\bar{a} \cdot \bar{c}}$
 $\bar{b} \bar{c} - \bar{d} = \frac{\bar{a} \cdot \bar{c}}{\bar{a} \cdot \bar{b}} \bar{b}$
 $\bar{d} = \bar{c} - \frac{\bar{a} \cdot \bar{c}}{\bar{a} \cdot \bar{b}} \bar{b}$

88. Ans: Statement-1 is true, Statement-2 is true;
Statement -2 is **not** a correct explanation
for Statement-1.

Sol: A (1, 0, 7) B, (1, 6, 3)

$$\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{5}$$

P ($\lambda, 2\lambda + 1, 3\lambda + 2$)

drs ($\lambda - 1, 2\lambda + 1, 3\lambda - 5$)

$$\therefore \lambda - 1 + 2(2\lambda + 1) + 3(3\lambda - 5) = 0$$

$$14\lambda - 14 = 0 \Rightarrow \lambda = 1$$

P (1, 3, 5) is mid point of A and B

Statement-1 is true

Statement-2 is also true but

statement-1 does not follow from 2

89. Ans: $\frac{3}{4} \leq A \leq 1$

$$\text{Sol: } A = \sin^2 x + \cos^4 x \\ = \cos^4 x - \cos^2 x + 1$$

$$= \left(\cos^2 x - \frac{1}{2} \right)^2 + \frac{3}{4}$$

$$\therefore \frac{3}{4} \leq A \leq 1$$

90. Ans: 2

$$\text{Sol: } \begin{vmatrix} 4 & k & 2 \\ k & 4 & 1 \\ 2 & 2 & 1 \end{vmatrix} = 0$$

$$4(4 - 2) - k(k - 2) + 2(2k - 8) = 0$$

$$= 8 - k^2 + 2k + 4k - 16 = 0$$

$$\Rightarrow -k^2 + 6k - 8 = 0$$

$$k^2 - 6k + 8 = 0$$

$$\Rightarrow (k - 4)(k - 2) = 0$$

$$\Rightarrow k = 2, 4$$

$$\therefore k = 2$$

