

# SOLUTIONS & ANSWERS FOR AIEEE-2011 VERSION – Q

## PART – A – PHYSICS

1. Ans: Wave moving in  $-x$  direction with speed

$$\sqrt{\frac{b}{a}}$$

Sol:  $y(x, t) = e^{-(\sqrt{a}x + \sqrt{b}t)^2}$   
This is of the form  $y(x, t) = f(x + vt)$ , where  
 $v = \frac{\sqrt{b}}{\sqrt{a}}$  travels in negative  $x$  direction.

2. Ans: 0.052 cm

Sol:  $LC = \frac{1}{100} = 0.01 \text{ mm}$   
Reading = PSR  $\times$  pitch + CSR  $\times$  LC  
= 0 + 52  $\times$  0.01  
= 0.52 mm  
= 0.052 cm

3. Ans:  $\frac{2}{3}g$

Sol:  $mg - T = ma$   
 $TR = \frac{mR^2}{2} \cdot \frac{a}{R}$   
 $\Rightarrow mg = \frac{3}{2}ma$   
 $\Rightarrow a = \frac{2}{3}g$

4. Ans: 0.4 $\pi$  mJ

Sol:  $E = T \cdot 8\pi(r_2^2 - r_1^2)$   
=  $8\pi T \left( \frac{25}{10^4} - \frac{9}{10^4} \right)$   
=  $8 \times 16 \times \pi \times 0.03 \times 10^{-4}$   
= 0.4 $\pi$  mJ

5. Ans: First increases and then decreases.

Sol: Angular momentum is conserved.  
I decreases  $\omega$  increases then I increases  
 $\omega$  decreases.

6. Ans:  $\frac{\pi}{2}$

Sol: Particle 1 is at equilibrium position ( $\phi = 0$ ).

maximum position.

Particle 2 is at

$$\left( \phi = \frac{\pi}{2} \right)$$

7. Ans:  $\frac{-9Gm}{r}$

Sol:  $\frac{Gm}{x^2} = \frac{G4m}{(r-x)^2}$   
 $\frac{(r-x)^2}{x^2} = 4$   
 $r - x = 2x$   
 $x = \frac{r}{3}$   
 $V = \frac{-Gm}{r} - \frac{G4m}{\frac{2r}{3}}$   
=  $-\frac{Gm}{r}(3+6)$   
=  $\frac{-9Gm}{r}$

8. Ans:  $v \propto x$

Sol:  $T \cos\theta = mg$   
 $T \sin\theta = F$   
 $\tan\theta = \frac{F}{mg}$   
 $\frac{x}{2\lambda} = \frac{F}{mg}$   
 $F \propto x$   
 $\int v dv \propto \int x dx$   
 $v^2 \propto x^2$   
 $v \propto x$

9. Ans: 0.15 mV

Sol:  $\mathcal{E} = B\lambda v$   
=  $5 \times 10^{-5} \times 2 \times 1.50$   
= 0.15 mV

10. Ans: 2 s

Sol:  $\frac{dv}{dt} = -2.5\sqrt{v}$   
 $\frac{dv}{\sqrt{v}} = -2.5 dt$   
 $\Rightarrow -2.5t = \left[ 2\sqrt{v} \right]_{6.25}^0$   
 $t = \frac{2\sqrt{6.25}}{2.5}$

$$= \frac{2 \times 2.5}{2.5} = 2$$

11. Ans:  $\frac{\pi}{4} \sqrt{LC}$

Sol:  $q' = q_0 \cos \omega t$

$$E = \frac{q_0^2}{2C}$$

$$\frac{E}{2} = \frac{1}{2} \frac{q_0^2}{2C}$$

i.e.  $q' = \frac{q_0}{\sqrt{2}}$

$$\frac{q_0}{\sqrt{2}} = q_0 \cos \omega t$$

$$\Rightarrow \omega t = \frac{\pi}{4}$$

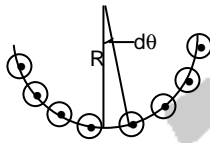
$$t = \frac{\pi}{4} \sqrt{LC}$$

12. Ans:  $45^\circ$

Sol:  $\mu_1 [\hat{N} \times K_1] = \mu_2 [\hat{N} \times K_2]$ . But plane of separation need to be XY.

13. Ans:  $\frac{\mu_0 I}{\pi^2 R}$

Sol:  $B = \frac{I}{\pi R} R d\theta \frac{\mu_0}{2\pi R} \sin \theta$



$$= \frac{\mu_0 I}{2\pi^2 R} \int_0^{\pi/2} \sin \theta d\theta$$

$$= \frac{\mu_0 I}{\pi^2 R}$$

14. Ans:  $\frac{1}{2} \frac{Mv^2(\gamma-1)}{R}$

Sol: Volume is constant

$$C_v = \frac{R}{(\gamma-1)}$$

$$KE = \frac{1}{2} Mv^2$$

$$\Delta Q = nC_v \Delta \theta = 1 \times C_v \Delta \theta$$

$$\therefore \Delta \theta = \frac{KE}{C_v} = \frac{1}{2} \frac{Mv^2(\gamma-1)}{R}$$

15. Ans:  $\left(\frac{M+m}{M}\right)^{1/2}$

Sol:  $Mv_1 = (M+m)v_2$

$$\frac{v_1}{v_2} = \frac{M+m}{M}$$

$$\frac{1}{2}(M+m)v_2^2 = \frac{1}{2}KA_2^2$$

$$\frac{1}{2}Mv_1^2 = \frac{1}{2}KA_1^2$$

$$\frac{1}{2}Mv_1^2 = \frac{1}{2}KA_1^2$$

$$\Rightarrow \frac{A_1^2}{A_2^2} = \frac{M}{M+m} \left(\frac{M+m}{M}\right)^2$$

$$= \frac{M+m}{M}$$

$$\therefore \frac{A_1}{A_2} = \left(\frac{M+m}{M}\right)^{1/2}$$

16. Ans:  $3.6 \times 10^{-3} \text{ m}$

Sol:  $P_0 + \frac{1}{2}\rho v_1^2 + \rho gh$

$$= P_0 + \frac{1}{2}\rho v_2^2$$

$$\Rightarrow 2gh = (v_2^2 - v_1^2)$$

$$\Rightarrow 2gh + v_1^2 = v_2^2;$$

$$v_1 = 0.4 \text{ m s}^{-1}, h_2 = 0.2 \text{ m}$$

$$\Rightarrow v_2 = 2.0396 \text{ m s}^{-1}$$

$$A_1 v_1 = A_2 v_2 \Rightarrow d_2^2 = \frac{d_1^2 v_1}{v_2}$$

$$\Rightarrow d_2 = d_1 \sqrt{\frac{v_1}{v_2}}$$

$$= 8 \times 10^{-3} \times \sqrt{\frac{0.4}{2.0396}}$$

$$\approx 3.6 \times 10^{-3} \text{ m}$$

17. Ans: Statement 1 is true. Statement 2 is true. and statement 2 is the correct explanation for statement - 1.

Sol: Statement 1 is true. Statement 2 is true. and statement 2 is the correct explanation for statement - 1.

18. Ans:  $\frac{n_1 T_1 + n_2 T_2 + n_3 T_3}{n_1 + n_2 + n_3}$

Sol:  $P_1 V = n_1 K T_1$

$$P_2 V = n_2 K T_2$$

$$P_3 V = n_3 K T_3$$

$$\frac{1}{2} m v^2 = \frac{3}{2} K T_1 \times n_1 + \frac{3}{2} K T_2 \times n_2 + \frac{3}{2} K T_3 \times n_3$$

$$= \frac{3}{2} K (n_1 + n_2 + n_3) T$$

$$T = \frac{n_1 T_1 + n_2 T_2 + n_3 T_3}{n_1 + n_2 + n_3}$$

19. Ans: more than 3 but less than 6.

Sol:  $\tau = Fr = 40t - 10t^2$   
 $\alpha = \frac{\tau}{I} = 4t - t^2$   
 $\frac{d\omega}{dt} = 4t - t^2 \Rightarrow \omega = 2t^2 - \frac{t^3}{3}$   
 (At  $t = 0, \omega = 0$ )  
 At  $t = 6$  s.  $\omega$  again become zero  
 $\omega = \frac{d\theta}{dt} = 2t^2 - \frac{t^3}{3} \Rightarrow \theta = \frac{2t^3}{3} - \frac{t^4}{12}$   
 $\therefore \theta$  in 6 s =  $(144 - 108) = 36$  rad  
 $\Rightarrow N = \frac{\theta}{2\pi} = \frac{36}{2\pi} = 5.72$  rotation.

20. Ans:  $2.7 \times 10^6 \Omega$

Sol:  $V = V_0(1 - e^{-t/RC})$   
 $120 = 200(1 - e^{-t/RC})$   
 $e^{-t/RC} = \frac{2}{5}$   
 $e^{t/RC} = 2.5$   
 $\frac{t}{RC} = 0.4 \times 2.5 \times 2.303$   
 $\Rightarrow R = 2.7 \times 10^6 \Omega$

21. Ans: 372 K and 310 K

Sol:  $1 - \frac{T_2}{T_1} = \frac{1}{6}$   
 $1 - \frac{T_2 - 62}{T_1} = \frac{1}{3}$   
 $\frac{T_2}{T_1} = \frac{5}{6}$   
 $\frac{T_2 - 62}{T_1} = \frac{2}{3}$   
 $\frac{T_2}{T_2 - 62} = \frac{5}{4}$   
 $4T_2 = 5T_2 - 310$   
 $T_2 = 310$  K  
 $\Rightarrow T_1 = 372$  K

22. Ans: Increases by 0.2%

Sol:  $R \propto \lambda^2$   
 $R' \propto \lambda'^2$   
 $\propto (1.001)^2 \lambda^2$   
 $\frac{\Delta R}{R} = 0.002$   
 $\therefore 0.002 \times 100$   
 $= 0.2\%$

23. Ans: Statement-1 is true, Statement-2 is true and Statement -2 is not the correct explanation of statement - 1

Sol: Statement-1 is true, Statement-2 is true and Statement -2 is not the correct explanation of statement - 1

24. Ans:  $\frac{1}{15^2} \times 15 = \frac{1}{15} \text{ m s}^{-1}$

Sol:  $\frac{1}{v} + \frac{1}{-2.8} = \frac{1}{0.2}$   
 $\Rightarrow \frac{1}{v} = \frac{15}{2.8}$   
 $v = \frac{2.8}{15}$   
 $\frac{v}{u} = \frac{1}{15}$   
 $\frac{v^2}{u^2} = \frac{1}{15^2}$   
 $\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$   
 $\Rightarrow \frac{dv}{du} = -\frac{v^2}{u^2}$   
 $\left| \frac{dv}{dt} \right| = \frac{v^2}{u^2} \cdot \frac{du}{dt}$   
 $= \frac{1}{15^2} \times 15 = \frac{1}{15} \text{ m s}^{-1}$

25. Ans: 108.8 eV

Sol:  $\frac{13.6 Z^2}{n^2} = 13.6 \times 9 \left[ 1 - \frac{1}{9} \right]$   
 $= 13.6 \times 9 \times \frac{8}{9}$   
 $= 108.8 \text{ eV}$

26. Ans:  $-6 \epsilon_0 a$

Sol:  $V = ar^2 + b$   
 $E = -\frac{dV}{dr} = -2ar$   
 $4\pi r^2 \cdot E = \frac{Q}{\epsilon_0}$   
 $Q = -4\pi r^2 \cdot 2ar \cdot \epsilon_0$   
 $\rho = \frac{-8\pi ar^3 \epsilon_0}{\frac{4}{3} \pi r^3}$   
 $= -6 \epsilon_0 a$

27. Ans:  $\frac{\pi v^4}{g^2}$

Sol:  $R_{\max} = \frac{v^2}{g}$   
 $\text{Area} = \pi(R_{\max})^2$   
 $= \frac{\pi v^4}{g^2}$

28. Ans: 8.4 kJ

Sol:  $\Delta U = mC\Delta T$   
 $= 4184 \times 20 \times 0.1$   
 $= 8.4 \text{ kJ}$

29. Ans: 20 min

Sol:  $N = \frac{N_0}{2^{t/T_{1/2}}}$   
 $\frac{N_0}{3} = \frac{N_0}{2^{t_2/20}} \Rightarrow t_2 = 20 \frac{\log 3}{\log 2}$   
 $N_0 \frac{2}{3} = \frac{N_0}{2^{t_1/20}} \Rightarrow t_1 = \frac{20(\log 3 - \log 2)}{\log 2}$   
 $t_2 - t_1 = \frac{20}{\log 2} (\log 3 - \log 3 + \log 2)$   
 $= 20 \text{ min}$

30. Ans: Statement - 1 is false, Statement-2 is true.

Sol: If  $v \Rightarrow 2v$ ,  
 $V_0' > 2V_0$ , well known result  
 $\Rightarrow$  Statement 1 is wrong.  
 Statement 2 is true.

**Part - B - Mathematics**

31. Ans: Statement-1 is true, Statement-2 is false.

Sol: P is (-2, -2) and Q (-1, 2) since R bisect  $\angle POQ$ ,  $PR \perp RQ = OP : OQ$   
 $= \sqrt{4+4} : \sqrt{1+4} = \sqrt{8} : \sqrt{5}$   
 $\therefore$  Statement 1 is true  
 But statement 2 is false.

32. Ans:  $\frac{3}{4} \leq A \leq 1$

Sol:  $A = \sin^2 x + \cos^4 x$   
 $= \cos^4 x - \cos^2 x + 1$   
 $= \left(\cos^2 x - \frac{1}{2}\right)^2 + \frac{3}{4}$   
 $\therefore \frac{3}{4} \leq A \leq 1$

33. Ans: -144

Sol:  $(1 - x - x^2 + x^3)^6 = (1 - x)^6 (1 - x^2)^6$   
 $= (1 - 6x + \dots - 20x^3 \dots - 6x^5) x$

$(1 - 6x^2 + 75x^4 - 20x^6 \dots)$   
 $= 120 - 300 + 36$   
 $= 156 - 300 = -144$

34. Ans: Does not exist

Sol:  $\lim_{x \rightarrow 2} \sqrt{2} \left| \frac{\sin(x-2)}{(x-2)} \right|$   
 Limit does not exist

35. Ans: Statement-1 is true, Statement-2 is true; Statement -2 is a correct explanation for Statement-1.

Sol:  $x_1 + x_2 + x_3 + x_4 = 6$   
 $x_i \geq 0$   
 no. of ways =  ${}^9C_3$   
 $S_2$  is true  
 $S_1$  is true  
 $S_1$  follows from  $S_2$

36. Ans:  $-\left(\frac{d^2y}{dx^2}\right)\left(\frac{dy}{dx}\right)^{-3}$

Sol:  $\frac{d^2x}{dy^2} = \frac{d}{dy} \left(\frac{dx}{dy}\right)$   
 $= \frac{d}{dy} \left[ \frac{1}{\frac{dy}{dx}} \right]$   
 $= \frac{-1}{\left(\frac{dy}{dx}\right)^2} \cdot \frac{d}{dy} \left(\frac{dy}{dx}\right)$   
 $= \frac{-1}{\left(\frac{dy}{dx}\right)^2} \cdot \frac{d^2y}{dx^2} \cdot \left(\frac{dx}{dy}\right)$   
 $= -\left(\frac{d^2y}{dx^2}\right)\left(\frac{dy}{dx}\right)^{-3}$

37. Ans: 7

Sol:  $\frac{dy}{dx} = y + 3$   
 $\frac{dy}{y+3} = dx$   
 $\log(y+3) = x + c$   
 $\therefore y + 3 = c e^x$   
 $x = 0, y = 2 \Rightarrow c = 5$   
 $\therefore y = 5 e^x - 3$   
 $\therefore y(\log 2) = 5 e^{\log 2} - 3$   
 $= 5 \times 2 - 3 = 7$

38. Ans: Statement-1 is true, Statement-2 is true; Statement -2 is **not** a correct explanation for Statement-1.

Sol:  $A = (x, y) \quad y - x \in \mathbb{Z}$   
 $B = (x, y) \quad x = \alpha y \text{ for rational } \alpha$

$A : x - x = 0 \in Z \Rightarrow (x, x) \in A$  reflexive  
 $y - x \in Z \Rightarrow x - y \in Z$   
 $\Rightarrow (y, x) \in A$  symmetric  
 $y - x \in Z$  and  $z - y \in Z \Rightarrow z - x \in Z$   
 $\therefore (x, z) \in A$  transitive  
 $A$  is equivalence relation  
 Statement - 1 is true  
 $B : x = 1, x \Rightarrow (x, x) \in B$  reflexive  
 $x = \alpha y \Rightarrow y = \frac{1}{\alpha} x \quad \therefore (y, x) \in B$   
symmetric  
 $x = \alpha y$  and  $y = \alpha z \Rightarrow x = \alpha^2 z$   
 $\therefore (x, z) \in B$  transitive  
 $B$  is equivalence relation  
 Statement - 2 is true but I does not follow from 2.

$$\begin{aligned}
 n^2 + 9n - 532 &= 0 \\
 n &= \frac{9 \pm \sqrt{81 + 2128}}{2} \\
 &= \frac{-9 \pm \sqrt{2209}}{2} = \frac{-9 \pm 47}{2} \\
 &= 19
 \end{aligned}$$

Therefore, answer is 21 months

39. Ans:  $\pi \log 2$

Sol:  $I = 8 \int_0^1 \frac{\log(1+x)}{1+x^2} dx$

$$\begin{aligned}
 &= 8 \int_0^{\pi/4} \text{Log}(1 + \tan \theta) d\theta \\
 &= \pi \log 2
 \end{aligned}$$

40. Ans:  $\beta \in (1, \infty)$

Sol: If  $1 + ai$  is root ( $a$ , real)  
 Then  $(1 + ia)^2 + \alpha(1 + ia) + \beta = 0$   
 $2a + \alpha a = 0 \Rightarrow \alpha = -2$   $a \neq 0$   
 $1 - a^2 + \alpha + \beta = 0$   
 $1 - a^2 + \beta = 0$   
 $\beta = a^2 + 1 > 1 \therefore \beta \in (1, \infty)$

41. Ans:  $\left[0, \frac{1}{2}\right]$

Sol:  $1 - P^5 \geq \frac{31}{32}$

$$\begin{aligned}
 P^5 &\leq 1 - \frac{31}{32} \\
 &\leq \frac{1}{32} \\
 P &\leq \frac{1}{2} = \left[0, \frac{1}{2}\right] \\
 \text{Choice (3)}
 \end{aligned}$$

42. Ans: 21 months

Sol: Total savings = 11040  
 Savings in the first 2 months = 400  
 Hence, savings in the next  $n$  months = 10640

We have

$$\begin{aligned}
 \frac{n}{2} [400 + (n-1)40] &= 10640 \\
 [200 + (n-1)20] n &= 10640 \\
 200n + 20n^2 - 20n &= 10640 \\
 20n^2 + 180n - 10640 &= 0
 \end{aligned}$$

43. Ans:  $(-\infty, 0)$

Sol:  $|x| - x > 0$   
 $\Rightarrow |x| > x$   
 $\Rightarrow x \in (-\infty, 0)$

44. Ans:  $\frac{2}{3}$

Sol: The angle is  $\sin^{-1} \frac{3}{\sqrt{14}}$

$$\begin{aligned}
 \therefore \frac{1+4+3\lambda}{\sqrt{(1+4+\lambda^2)(1+4+9)}} &= \frac{3}{\sqrt{14}} \\
 14(3\lambda+5)^2 &= 9 \times 14(5+\lambda^2) \\
 9\lambda^2 + 30\lambda + 25 &= 9\lambda^2 + 45 \\
 \Rightarrow 30\lambda &= 20 \Rightarrow \lambda = \frac{2}{3}
 \end{aligned}$$

45. Ans: -5

Sol:  $|a| = |b| = 1$   $a, b = 0$   
 $(2a - b) \cdot ((a \times b) \times (a + 2b))$   
 $= (2a - b) \times$   
 $[(a \cdot a) b - (a \cdot b) a + (2b \cdot a) b - (2b \cdot b)]$   
 $(2a - b) \cdot (b - 2a) = -5$

46. Ans:  $3x^2 + 5y^2 - 32 = 0$

Sol:  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$

$$\begin{aligned}
 \frac{9}{a^2} + \frac{1}{b^2} &= 1 \\
 \frac{1}{b^2} &= 1 - \frac{9}{a^2} \\
 \frac{1}{a^2(1-\frac{9}{a^2})} &= \frac{a^2-9}{a^2} \\
 a^2 - 9 &= \frac{3}{5} \\
 a^2 &= 9 + \frac{3}{5} = \frac{32}{5} \\
 b^2 &= a^2 \times \frac{3}{5} = \frac{32}{5} \times \frac{3}{5} = \frac{32}{5} \\
 \text{Equation of the ellipse is} \\
 \frac{x^2}{\frac{32}{5}} + \frac{y^2}{\frac{32}{5}} &= 1 \\
 3x^2 + 5y^2 - 32 &= 0
 \end{aligned}$$

47. Ans:  $I - \frac{kT^2}{2}$

Sol:  $\frac{dv(t)}{dt} = -k(T-t)$

$V(t) = \int -k(T-t) dt$

$\frac{k(T-t)^2}{2} + C$

$t = 0, V(t) = I$

$\Rightarrow I = \frac{kT^2}{2} + C$

$C = I - \frac{kT^2}{2}$

Therefore,

$V(t) = \frac{k(T-t)^2}{2} + I - \frac{kT^2}{2}$

$\Rightarrow V(T) = 0 + I - \frac{kT^2}{2}$

$= I - \frac{kT^2}{2}$

48. Ans:  $\bar{c} - \frac{\bar{a} \cdot \bar{c}}{\bar{a} \cdot \bar{b}}$

Sol:  $\bar{b} \times \bar{c} = \bar{b} \times \bar{d}$

$\bar{a} \cdot \bar{d} = 0$

$\bar{b} \times (\bar{c} - \bar{d}) = 0$

$\bar{b}$  and  $(\bar{c} - \bar{d})$  are collinear

$\bar{b} = k(\bar{c} - \bar{d})$

$\bar{a} \cdot \bar{b} = k(\bar{c} - \bar{d}) \cdot \bar{a}$

$k \frac{[\bar{c} - \bar{d}]}{[\bar{c} - \bar{c}]}$

$k = \frac{\bar{a} \cdot \bar{b}}{\bar{a} \cdot \bar{c}}$

$\bar{b} \cdot \bar{c} - \bar{d} = \frac{\bar{a} \cdot \bar{c}}{\bar{a} \cdot \bar{b}} \bar{b}$

$\bar{d} = \bar{c} - \frac{\bar{a} \cdot \bar{c}}{\bar{a} \cdot \bar{b}} \bar{b}$

49. Ans:  $|a| = c$

Sol: Two circle should touch each other

Centres are  $(\frac{a}{2}, 0)$  and  $(0, 0)$

$\therefore$  also second circle passes through  $(0, 0)$

$\therefore c = a \Rightarrow |a| = c$

50. Ans:  $P(C|D) \geq P(C)$

Sol:  $P(C|D) = \frac{P(CD)}{P(D)}$

$= \frac{P(C)}{P(D)}$

$\geq P(C)$

51. Ans: 2

Sol:  $\begin{vmatrix} 4 & k & 2 \\ k & 4 & 1 \\ 2 & 2 & 1 \end{vmatrix} = 0$

$4(4-2) - k(k-2) + 2(2k-8) = 0$

$= 8 - k^2 + 2k + 4k - 16 = 0$

$\Rightarrow -k^2 + 6k - 8 = 0$

$k^2 - 6k + 8 = 0$

$\Rightarrow (k-4)(k-2) = 0$

$\Rightarrow k = 2, 4$

$\therefore k = 2$

52. Ans:  $\sim (Q \leftrightarrow (P \wedge \sim R))$

Sol: The given statement is

$(P \wedge \sim R) \leftrightarrow Q \equiv Q \leftrightarrow (P \wedge \sim R)$

$\therefore$  The required negative is

$\sim [Q \leftrightarrow (P \wedge \sim R)]$

53. Ans:  $\frac{3\sqrt{2}}{8}$

Sol: Slope of the line perpendicular to  $y - x = 1$  is  $(-1)$

Hence  $t = 1$

Point on the parabola corresponding to  $t = 1$  is

$\Rightarrow \left(\frac{1}{4}, \frac{1}{2}\right)$

$\therefore$  shortest distance  $= \frac{\frac{1}{4} - \frac{1}{2} + 1}{\sqrt{2}} = \frac{3\sqrt{2}}{8}$

54. Ans: 4

Sol: Median  $= \frac{25a + 26b}{2}$

$= \frac{51a}{2}$

Numerical value of the sum of the derivation

$= \left| 2a \left\{ \frac{1}{2} + \frac{3}{2} + \frac{5}{2} + \dots + \frac{49}{2} \right\} \right|$

$= \left| \frac{2a \times 25^2}{2} \right| = |25^2 a|$

Mean derivation about median  $= \left| \frac{25^2 a}{50} \right|$

$\left| \frac{25^2 a}{50} \right| = 50$

$|a| = \frac{50 \times 50}{25 \times 25} = 4$

55. Ans: Statement-1 is true, Statement-2 is true; Statement -2 is **not** a correct explanation for Statement-1.

Sol: A (1, 0, 7) B, (1, 6, 3)

$$\frac{x}{1} = \frac{y-1}{2} = \frac{2-2}{5}$$

$$P(\lambda, 2\lambda + 1, 3\lambda + 2)$$

$$\text{drs } (\lambda - 1, 2\lambda + 1, 3\lambda - 5)$$

$$\therefore \lambda - 1 + 2(2\lambda + 1) + 3(3\lambda - 5) = 0$$

$$14\lambda - 14 = 0 \Rightarrow \lambda = 1$$

P(1, 3, 5) is mid point of A and B

Statement-1 is true

Statement-2 is also true but

statement-1 does not follow from 2

56. Ans: Statement-1 is true, Statement-2 is true;  
Statement-2 is **not** a correct explanation  
for Statement-1.

Sol: if  $AB = BA$   
 $(AB)^T = A^T B^T$   
 $\Rightarrow AB$  is symmetric  
Statement-2 is true  
 $(ABA)^T = A^T B^T A^T$   
Take  $A = I$  and  $B =$  some non-symmetric  
 $\therefore ABA$  always  
 $\therefore A(BA)$  and  $(AB)A$  are symmetric  
Statement-1 is true but does not depend  
on Statement-2

57. Ans: (1, 1)

Sol:  $(1 + \omega)^7 = A + B\omega$   
 $(-\omega^2)^7 = A + B\omega$   
 $-\omega^{14} = A + B\omega$   
 $-\omega^2 = A + B\omega$   
 $1 + \omega = A + B\omega$   
 $\therefore A = 1 \quad B = 1$   
 $\therefore (1, 1)$

58. Ans:  $p = -\frac{3}{2}, q = \frac{1}{2}$

$$\text{Sol: } f(x) = \frac{\sin(p+1)x + \sin x}{x}, x < 0$$

$$= q, x = 0$$

$$\frac{\sqrt{x+x^2} - \sqrt{x}}{x^{3/2}}, x > 0$$

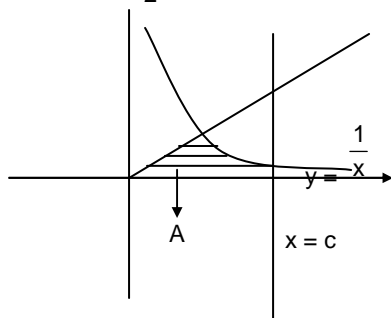
is continuous.

$$\Rightarrow p + 1 + 1 = q = \lim_{x \rightarrow 0} \frac{x}{x^{3/2}(\sqrt{x+x^2} + \sqrt{x})}$$

$$= \frac{1}{2}$$

$$\therefore p = -\frac{3}{2}, q = \frac{1}{2}$$

59. Ans:  $\frac{3}{2}$  square units



$$\text{Sol: } y = x$$

$$y = \frac{1}{x} \Rightarrow x^2 = 1$$

$$\Rightarrow x = 1 (x > 0)$$

$$y = \frac{1}{x}, x = e \Rightarrow x = e$$

$$\therefore \text{area } A = \int_1^e \left(x - \frac{1}{x}\right) dx$$

$$= \frac{e^2 - 1}{2} - \log e$$

$$= \frac{e^2 - 3}{2}$$

$$\text{Required area} = \frac{1}{2} \cdot e^2 - \frac{e^2 - 3}{2} = \frac{3}{2}$$

60. Ans: local maximum at  $\pi$  and local minimum at  $2\pi$

$$\text{Sol: } f'(x) = \sqrt{x} \sin x$$

$$f''(x) = \frac{2x \cos x + \sin x}{2\sqrt{x}}$$

$$f'(x) = 0 \Rightarrow x = n\pi, n \in \mathbb{Z}$$

$$\text{ie., } x = \pi, 2\pi \text{ in } \left(0, \frac{5\pi}{2}\right)$$

$$f''(\pi) < 0 \text{ and } f''(2\pi) > 0$$

$$\therefore f(x) \text{ has maximum at } x = \pi$$

$$\text{And minimum at } x = 2\pi$$

## PART C – CHEMISTRY

61. Ans:  $AlCl_3$

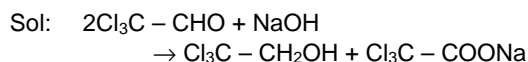
Sol: Fajan's rules.

$Al^{3+}$  is the smallest cation and it has high charge.

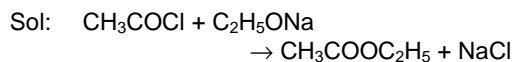
62. Ans:  $2^{nd}$

Sol: RNA contains  $\beta$ -D-ribose while DNA contains  $\beta$ -D-2-deoxyribose.

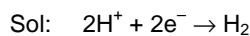
63. Ans: 2, 2, 2-Trichloroethanol



64. Ans: Ethyl ethanoate



65. Ans:  $p(H_2) = 2 \text{ atm}$  and  $[H^+] = 1.0 \text{ M}$



$$E_{Cl} = \frac{0.0591}{2} \log \frac{[H^+]^2}{[H_2]}$$

$$[H_2] > [H^+]^2$$

66. Ans:  $\text{CH}_3\text{CH}_2\text{CH}(\text{Cl})\text{CO}_2\text{H}$

Sol: Presence of Cl having  $-I$  effect on the  $\alpha$ -carbon makes 2-chlorobutanoic acid the strongest acid among the given compounds.

67. Ans:  $\alpha = \frac{i - 1}{(x + y - 1)}$

Sol:  $i = 1 - \alpha + n\alpha$ ;  $n = x + y$   
 $\alpha = \frac{i - 1}{x + y - 1}$

68. Ans:  $a$  for  $\text{Cl}_2 > a$  for  $\text{C}_2\text{H}_6$  but  $b$  for  $\text{Cl}_2 < b$  for  $\text{C}_2\text{H}_6$

Sol: 'a' is a measure of attraction between the molecules and 'b' the size of the molecules.

69. Ans: 1.8 atm

Sol:  $\text{CO}_2 + \text{C} \rightarrow 2\text{CO}$   
 $a - x \quad 2x$

$a = 0.5 \text{ atm}$

$a + x = 0.8 \text{ atm}$

$x = 0.3 \text{ atm}$

$K_p = \frac{p_{\text{CO}}^2}{p_{\text{CO}_2}} = \frac{(0.6)^2}{0.2} = 1.8 \text{ atm}$

70. Ans:  $\text{BF}_6^{3-}$

Sol: Boron cannot form  $\text{BF}_6^{3-}$  since boron has no available d-orbitals.

71. Ans: The complex is an outer orbital complex

Sol:  $[\text{Cr}(\text{NH}_3)_6]\text{Cl}_3$  is not an outer orbital complex.

72. Ans: 804.32 g

Sol:  $\Delta T_f = K_f \times \frac{W_2}{M_2} \times \frac{1}{W_1}$

$6 = 1.86 \times \frac{W_2}{62} \times \frac{1}{4}$

$W_2 = 800 \text{ g}$

Wt. of glycol required is more than 800 g

73. Ans:  $\text{Al}_2\text{O}_3 < \text{MgO} < \text{Na}_2\text{O} < \text{K}_2\text{O}$

Sol:  $\text{K}_2\text{O}$  is more basic than  $\text{Na}_2\text{O}$ .  $\text{Al}_2\text{O}_3$  is amphoteric.

74. Ans: 32 times

Sol: 2 times increase for  $10^\circ\text{C}$   
 $2^5 = 32$  times increase for  $50^\circ\text{C}$

75. Ans: 2.82 BM

Sol: There are two unpaired electrons in  $[\text{NiCl}_4]^{2-}$  hence the paramagnetic moment is 2.82 BM.

76. Ans:  $sp^2, sp, sp^3$

Sol:  $\text{NO}_3^- - sp^2, \text{NO}_2^+ - sp$  and  $\text{NH}_4^+ - sp^3$

77. Ans: Availability of 4f electrons results in the formation of compounds in +4 state for all the members of the series

Sol: All the lanthanoids does not exhibit +4 oxidation state.

78. Ans: 0.086

Sol: Mole fraction of methanol  
$$= \frac{\text{moles of methanol}}{\text{total moles}} = \frac{5.2}{5.2 + \frac{1000}{18}}$$
$$= 0.086$$

79. Ans: The stability of hydrides increases from  $\text{NH}_3$  to  $\text{BiH}_3$  in group 15 of the periodic table.

Sol: Stability of hydrides decreases from  $\text{NH}_3$  to  $\text{BiH}_3$ .

80. Ans:  $4f^7 5d^1 6s^2$

Sol: The outer electronic configuration of  ${}_{64}\text{Gd}$  is  $4f^7 5d^1 6s^2$

81. Ans: The oxidation state of sulphur is never less than +4 in its compounds

Sol: Sulphur exhibits oxidation state lower than +4 in its compounds.

82. Ans: pentagonal bipyramid

Sol:  $\text{IF}_7$  is pentagonal bipyramidal.

83. Ans: a vinyl group

Sol: Formation of  $\text{HCHO}$  in ozonolysis shows the presence of  $\text{CH}_2 = \text{CH} -$  group.

84. Ans: 743 nm

Sol:  $\frac{1}{355} = \frac{1}{680} - \frac{1}{\lambda}$   
 $\lambda = 743 \text{ nm}$

85. Ans: Acetaldehyde

Sol: Acetaldehyde reduces tollen's reagent to metallic silver on warming.



86. Ans: Neutral  $\text{FeCl}_3$

Sol: Neutral  $\text{FeCl}_3$  solution gives violet colour with phenol.

87. Ans: 2, 4, 6-Tribromophenol

Sol: Phenol forms 2, 4, 6-tribromophenol when treated with a mixture of  $\text{KBr}$ ,  $\text{KBrO}_3$  and  $\text{HCl}$ .

88. Ans:  $\text{A}_2\text{B}_5$

Sol:  $\text{A}_1\text{B}_5 / 2 = \text{A}_2\text{B}_5$

89. Ans:  $38.3 \text{ J mol}^{-1} \text{ K}^{-1}$

Sol:  $\Delta S = 2.303 nR \log \frac{V_2}{V_1}$   
 $= 2.303 \times 2 \times 8.314 \times \log 10$   
 $= 38.3 \text{ J K}^{-1}$

90. Ans: 2-Pentanone

